

Brute Force 1 Example

> restart

Element Equations

> OhmR1 := v1 = i1·R1:

> OhmR2 := v2 = i2·R2:

KCL Equations (Third one not used)

> KCLna := -ia + i1 + i2 = 0:

> KCLnb := -i2 + ib = 0:

> KCLnc := ia - i1 - ib = 0:

KVL Equations

> KVLl1 := -va + v1 = 0:

> KVLl2 := -v1 + v2 + vb = 0:

Symbolically Solve

> MySoln := simplify(expand(solve({ OhmR1, OhmR2, KCLna, KCLnb, KCLnc, KVLl1, KVLl2}, [i1, i2, ib, v1, v2, va])))

$$\begin{aligned} \text{MySoln} := & \left[\left[i1 = \frac{R2 ia + vb}{R1 + R2}, i2 = \frac{R1 ia - vb}{R1 + R2}, ib = \frac{R1 ia - vb}{R1 + R2}, v1 \right. \right. \\ & \left. \left. = \frac{R1 (R2 ia + vb)}{R1 + R2}, v2 = \frac{R2 (R1 ia - vb)}{R1 + R2}, va = \frac{R1 (R2 ia + vb)}{R1 + R2} \right] \right] \end{aligned} \quad (1)$$

Define and Substitute Numerical Values

> Vals := R1 = 1000 [[Ω]], R2 = 2.2e3 [[Ω]], ia = 5e-3 [[A]], vb = 12 [[V]]

$$\text{Vals} := R1 = 1000 \text{ [[}\Omega\text{]]}, R2 = 2200. \text{ [[}\Omega\text{]]}, ia = 0.005 \text{ [[A]], vb = 12 \text{ [[V]]} \quad (2)$$

> MyNumSoln := subs(Vals, MySoln)

$$\text{MyNumSoln} := \left[\left[i1 = \frac{0.0003125000000 (11.0 \text{ [[}\Omega\text{]] [[A]] + 12 \text{ [[V]])}}{\text{[[}\Omega\text{]]}}, i2 \right. \right. \quad (3)$$

$$= \frac{0.0003125000000 (5.000 \text{ [[}\Omega\text{]] [[A]] - 12 \text{ [[V]])}}{\text{[[}\Omega\text{]]}}, ib$$

$$= \frac{0.0003125000000 (5.000 \text{ [[}\Omega\text{]] [[A]] - 12 \text{ [[V]])}}{\text{[[}\Omega\text{]]}}, v1$$

$$= 3.437500000 \text{ [[}\Omega\text{]] [[A]] + 3.750000000 \text{ [[V]]}, v2 = 3.437500000 \text{ [[}\Omega\text{]] [[A]]$$

$$- 8.250000000 \text{ [[V]], va = 3.437500000 \text{ [[}\Omega\text{]] [[A]] + 3.750000000 \text{ [[V]]}] \quad (4)$$

> evalf[4](simplify(MyNumSoln))

$$\text{[[} i1 = 0.007188 \text{ [[A]], } i2 = -0.002188 \text{ [[A]], } ib = -0.002188 \text{ [[A]], } v1 = 7.188 \text{ [[V]], } \quad (4)$$

$$v2 = -4.812 \text{ [[V]], } va = 7.188 \text{ [[V]]}]$$

Define Auxiliary Equations

> AuxEqn := [pdelia = va·ia, pdelvb = -vb·ib, pabsR1 = v1·i1, pabsR2 = v2·i2,]:

> MySoln[1][]

$$\begin{aligned} i1 = & \frac{R2 ia + vb}{R1 + R2}, i2 = \frac{R1 ia - vb}{R1 + R2}, ib = \frac{R1 ia - vb}{R1 + R2}, v1 = \frac{R1 (R2 ia + vb)}{R1 + R2}, v2 \\ & = \frac{R2 (R1 ia - vb)}{R1 + R2}, va = \frac{R1 (R2 ia + vb)}{R1 + R2} \end{aligned} \quad (5)$$

Substitute in Symbolic Solutions to Auxiliary Variables

> *MyFinalAnswer* := *subs*(*MySoln*[1][], *AuxEqn*)

$$\text{MyFinalAnswer} := \left[\begin{aligned} p_{delia} &= \frac{R1 (R2 ia + vb) ia}{R1 + R2}, p_{delvb} = -\frac{vb (R1 ia - vb)}{R1 + R2}, \\ p_{absR1} &= \frac{R1 (R2 ia + vb)^2}{(R1 + R2)^2}, p_{absR2} = \frac{R2 (R1 ia - vb)^2}{(R1 + R2)^2} \end{aligned} \right] \quad (6)$$

Substitute in Symbolic Solutions then Numerical Values to Auxiliary Variables

> *MyFinalNumAnswer* := *subs*(*MySoln*[1][], *Vals*, *AuxEqn*)

$$\text{MyFinalNumAnswer} := \left[\begin{aligned} p_{delia} &= 0.001562500000 (11.0 \text{ } [\Omega] \text{ } [A]) \\ &+ 12 \text{ } [V]) \text{ } [A], p_{delvb} = \end{aligned} \right] \quad (7)$$

$$- \frac{0.003750000000 \text{ } [V] (5.000 \text{ } [\Omega] \text{ } [A] - 12 \text{ } [V])}{[\Omega]}, p_{absR1}$$

$$= \frac{0.00009765625000 (11.0 \text{ } [\Omega] \text{ } [A] + 12 \text{ } [V])^2}{[\Omega]}, p_{absR2}$$

$$= \frac{0.0002148437500 (5.000 \text{ } [\Omega] \text{ } [A] - 12 \text{ } [V])^2}{[\Omega]} \right]$$

> *evalf*[4](*simplify*(*MyFinalNumAnswer*))

$$\left[\begin{aligned} p_{delia} &= 0.03593 \text{ } [W], p_{delvb} = 0.02625 \text{ } [W], p_{absR1} = 0.05166 \text{ } [W], p_{absR2} \\ &= 0.01053 \text{ } [W] \end{aligned} \right] \quad (8)$$